

## An Example

Consider some relations and metadata below:

### Relations

- Student(SID, SLName, Dept)
- Course(CID, Dept, CName)
- Grade(SID, CID, Sem, Grade)

### Metadata

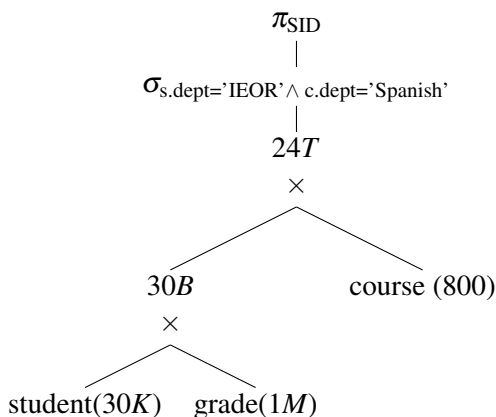
- 30,000 students (~300 IEOR majors, ~1%)
- 800 courses (16 Spanish courses, ~2%)
- 1,000,000 grade records (~30 per student)

A typical SQL query would look like:

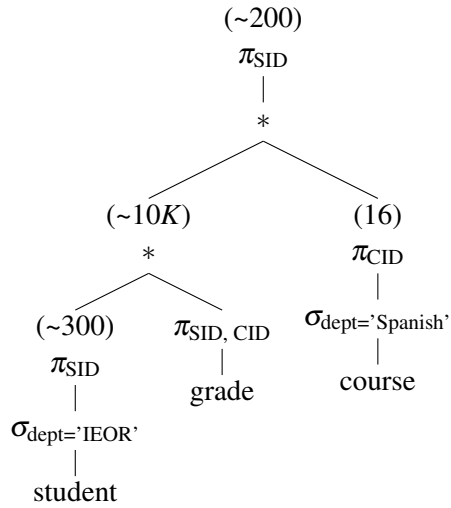
```

select distinct s.SID
from student s, course c, grade g
where s.dept = 'IEOR' and
       c.dept = 'Spanish' and
       c.CID = g.CID and
       s.SID = g.SID;
  
```

The query tree is shown below



Consider this optimized query tree instead:



## Equivalence Rules

1.  $\sigma_{c_1}(\sigma_{c_2}(\dots(\sigma_{c_n}(R)))) \Leftrightarrow \sigma_{c_1 \wedge c_2 \wedge \dots \wedge c_n}(R)$   
(CNF  $\equiv$  Conjunctive Normal Form) σ - CNF Rule
2.  $\sigma_{c_2}(\sigma_{c_1}(R)) \Leftrightarrow \sigma_{c_1}(\sigma_{c_2}(R))$  σ - commute Rule
3.  $\pi_{Amin}(R) \Leftrightarrow \pi_{Amin}(\pi_{A'}(\pi_{MaxA}(R)))$   
 $Amin \subset A' \subset MaxA$  π - minA Rule
4.  $R * (S * T) \Leftrightarrow (R * S) * T$  \* - Associative Rule
5.  $(T * R) * S \Leftrightarrow (R * S) * T$  \* - Commutative Rule
6.  $R - \sigma_c(R) \Leftrightarrow \sigma_{\neg c}(R)$  ¬ Rule

## CNF

- A **disjunct** is a wff that contains only  $\vee$  and  $\neg$  connectives. E.g.  $\neg p \vee q$   
Note that formulas can be converted into disjuncts. E.g.  $p \rightarrow q \models \neg p \vee q$
- A **conjunct** is a wff that contains only  $\wedge$  and  $\neg$  connectives
- A **wff is in CNF** if it is a single disjunct or a set of disjuncts joined by  $\wedge$ .  
For example,  $(\varphi_1 \vee \neg \varphi_2) \wedge (\varphi_1 \vee \varphi_3) = \{\varphi_1 \vee \neg \varphi_2, \varphi_1 \vee \varphi_3\}$

### Recap: DeMorgan's Rules

- $\neg(c_1 \wedge c_2) \equiv \neg c_1 \vee \neg c_2$
- $\neg(c_1 \vee c_2) \equiv \neg c_1 \wedge \neg c_2$

## Optimization Algorithm

1. For each  $\sigma$  put into CNF, reorder them so that the most selective conditions are applied first.
2. If you have  $R \bowtie_{C_R \wedge C_S} S$ , change it to  $\sigma_{C_R}(R) * \sigma_{C_S}(S)$ .  
Move highly selective  $\sigma$  as far down the query tree as possible.
3. Push the projections ( $\pi$ ) as far down as possible.